

Multiplying Rational Expressions Involving Polynomials

A **polynomial** is the SUM/DIFFERENCE of one or more binomials. You **MUST** consider them as a **GROUP** when factoring.

1. $\frac{4x^2 - 4x}{x^2 + 2x - 3} \cdot \frac{x^2 + x - 6}{4x}$

$$\frac{4x(x-1)}{(x-1)(x+3)} \cdot \frac{(x-2)(x+3)}{4x} = \boxed{(x-2)}$$

$\rightarrow \begin{array}{r} -3 \\ 2 \end{array} \overline{) x^2 + 3x - 1x - 3}$
 $\rightarrow \begin{array}{r} -3 \\ 2 \end{array} \overline{) x(x+3) - 1(x+3)}$

2. $\frac{27x^3 - 3x}{3x^2 - 2x - 1} \cdot \frac{3x^2 - 4x + 1}{3x}$

$$\frac{3x(9x^2 - 1)}{(3x+1)(x-1)} \cdot \frac{(3x-1)(x-1)}{3x}$$

$\rightarrow \begin{array}{r} 3 \\ -3 \\ -4 \end{array} \overline{) 3x^2 - 3x - 1x + 1}$
 $\rightarrow \begin{array}{r} 3 \\ -3 \\ -4 \end{array} \overline{) 3x(x-1) - 1(x-1)}$

$\rightarrow \begin{array}{r} -9 \\ 3 \\ 0 \end{array} \overline{) 9x^2 + 3x - 3x - 1}$
 $\rightarrow \begin{array}{r} -9 \\ 3 \\ 0 \end{array} \overline{) 3x(3x+1) - 1(3x+1)}$

3. $\frac{x+3}{4x^2 + 7x - 15} \cdot 4x+5$

$$\frac{(x+3)}{(4x-5)(x+3)} \cdot \frac{(4x+5)}{1} = \boxed{\frac{(4x+5)}{(4x-5)}}$$

$\rightarrow \begin{array}{r} -60 \\ 12 \\ 7 \end{array} \overline{) 4x^2 + 12x - 5x - 15}$
 $\rightarrow \begin{array}{r} -60 \\ 12 \\ 7 \end{array} \overline{) 4x(x+3) - 5(x+3)}$

$\rightarrow \begin{array}{r} -3 \\ -3 \\ -2 \end{array} \overline{) 3x^2 - 3x + 1x - 1}$
 $\rightarrow \begin{array}{r} -3 \\ -3 \\ -2 \end{array} \overline{) 3x(x-1) - 1(x-1)}$

$$\frac{3x(3x+1)(3x-1)}{(3x+1)(x-1)} \cdot \frac{(3x-1)(x-1)}{3x}$$

$$\boxed{(3x-1)(3x-1)}$$

4. $\frac{2x^2 - 4x}{x^2 - 5x + 6} \cdot \frac{x^2 - 4x + 3}{2x}$

$$\frac{2x(x-2)}{(x-2)(x-3)} \cdot \frac{(x-1)(x-3)}{2x} = \boxed{(x-1)}$$

$\rightarrow \begin{array}{r} 6 \\ -3 \\ -5 \end{array} \overline{) x^2 - 3x - 2x + 6}$
 $\rightarrow \begin{array}{r} 6 \\ -3 \\ -5 \end{array} \overline{) x(x-3) - 2(x-3)}$

$\rightarrow \begin{array}{r} 3 \\ -3 \\ -4 \end{array} \overline{) x^2 - 3x - 1x + 3}$
 $\rightarrow \begin{array}{r} 3 \\ -3 \\ -4 \end{array} \overline{) x(x-3) - 1(x-3)}$

Steps:

- 1) Factor the numerators and denominators separately
- 2) Multiply- leave as a product of factors
- 2) Cancel out any factors that are in common to both the numerator and denominator

Dividing Rational Expression

~~a.c.~~
~~b~~

Diving by a rational expression is the same as

multiplying by the reciprocal

$$\begin{array}{r} \cancel{8} \quad \cancel{4} \quad \cancel{2} \quad \cancel{8} \\ \cancel{4} \quad \cancel{2} \quad \cancel{2} \quad \cancel{4} \\ \hline \end{array} \rightarrow \begin{array}{r} x^2 - 4x - 2x + 8 \\ x(x-4) - 2(x-4) \end{array}$$

$$1. \frac{5x}{3x-12} \div \frac{x^2-2x}{x^2-6x+8} = \frac{5x}{3x-12} \cdot \frac{x^2-6x+8}{x^2-2x}$$

$$\frac{5\cancel{x}}{3\cancel{(x-4)}} \cdot \frac{\cancel{(x-2)}\cancel{(x-4)}}{x\cancel{(x-2)}} = \boxed{\frac{5}{3}}$$

Steps:

- 1) "Flip" the 2nd fraction.
- 2) Factor the numerators and denominators separately.
- 3) Multiply- leave as a product of factors
- 4) Cancel out any factors that are in common to both the numerator and denominator

$$2. \frac{8x^2+10x-3}{4x^2} \div (4x^2-x) = \frac{8x^2+10x-3}{4x^2} \cdot \frac{1}{4x^2-x}$$

$$\frac{\cancel{(4x-1)}(2x+3)}{4x^2} \cdot \frac{1}{x\cancel{(4x-1)}} = \boxed{\frac{2x+3}{4x^3}}$$

$$\begin{array}{r} -24 \\ 12 \quad -2 \quad \rightarrow 8x^2+12x-2x-3 \\ \hline 10 \quad 4x(2x+3) - 1(2x+3) \end{array}$$

$$3. \frac{3}{4x-8} \div \frac{x^2+3x}{x^2+x-6}$$

$$\frac{3}{4(x-2)} \cdot \frac{x^2+x-6}{x^2+3x}$$

$$\frac{3}{4\cancel{(x-2)}} \cdot \frac{\cancel{(x-2)}(x+3)}{x(x+3)} = \boxed{\frac{3}{4x}}$$

$$\begin{array}{r} -6 \\ 3 \quad -2 \quad \rightarrow x^2+3x-2x-6 \\ \hline 1 \quad x(x+3) - 2(x+3) \end{array}$$

$$4. \frac{x}{x+3} \cdot (4x+1) \div \frac{16x^2-1}{x+3}$$

$$\frac{x}{x+3} \cdot \frac{(4x+1)}{1} \cdot \frac{(x+3)}{16x^2-1} = \frac{x}{\cancel{(x+3)}} \cdot \frac{\cancel{(4x+1)}}{1} \cdot \frac{\cancel{(x+3)}}{(4x-1)\cancel{(4x+1)}} = \boxed{\frac{x}{4x-1}}$$

$$\begin{array}{r} -16 \\ 4 \quad -4 \quad \rightarrow 16x^2+4x-4x-1 \\ \hline 0 \quad 4x(4x+1) - 1(4x+1) \end{array}$$