

Part 1 Name: KEY

Topic: 8.5 Properties of Logarithms (part 1)

Summary:

Complete the table below.

$\log_b m$	$\log_b n$	$\log_b mn$
$\log 10 = 1$	$\log 100 = 2$	$\log(10 * 100) = 3$
$\log 0.1 = -1$	$\log 0.01 = -2$	$\log(0.1 * 0.01) = -3$
$\log_2 4 = 2$ *since $2^2=4$	$\log_2 8 = 3$ *Since $2^3=8$	$\log_2(4 * 8) = 5$ *since $2^5=32$

Do you notice a pattern when you compare the first two columns to the third column?

The first column plus the second column equals the third column.

Properties of Logarithms

Product Property:

$$\log_b mn = \log_b m + \log_b n$$

Quotient Property:

$$\log_b \frac{m}{n} = \log_b m - \log_b n$$

Power Property:

$$\log_b m^n = n \log_b m$$

Use $\log_9 5 \approx 0.732$ and $\log_9 11 \approx 1.091$ to approximate the following.

1. $\log_9 \frac{5}{11}$

$$\log_9 5 - \log_9 11$$

$$0.732 - 1.091$$

$$\boxed{-0.359}$$

2. $\log_9 55$

$$\log_9 (5 \cdot 11)$$

$$\log_9 5 + \log_9 11$$

$$0.732 + 1.091$$

$$\boxed{1.823}$$

3. $\log_9 25$

$$\log_9 (5 \cdot 5)$$

$$\log_9 5 + \log_9 5$$

$$0.732 + 0.732$$

$$\boxed{1.464}$$

Use $\log_5 3 \approx 0.683$ and $\log_5 7 \approx 1.209$ to approximate the following.

4. $\log_5 \frac{7}{3}$

$$\log_5 7 - \log_5 3$$

$$1.209 - 0.683$$

$$\boxed{0.526}$$

5. $\log_5 9$

$$\log_5 (3 \cdot 3)$$

$$\log_5 3 + \log_5 3$$

$$0.683 + 0.683$$

$$\boxed{1.366}$$

6. $\log_5 27$

$$\log_5 (3 \cdot 3 \cdot 3)$$

$$\log_5 (3) + \log_5 3 +$$

$$\log_5 3 =$$

$$0.683 + 0.683 +$$

$$0.683 = \boxed{2.049}$$

Use $\log 2 \approx 0.301$ and $\log 7 \approx 0.845$ to approximate the following.

7. $\log 4$

$$\log (2 \cdot 2)$$

$$\log 2 + \log 2$$

$$0.301 + 0.301$$

$$\boxed{0.602}$$

8. $\log 14$

$$\log (2 \cdot 7)$$

$$\log 2 + \log 7$$

$$0.301 + 0.845$$

$$\boxed{0.146}$$

9. $\log \frac{7}{2}$

$$\log 7 - \log 2$$

$$0.845 - 0.301$$

$$\boxed{0.544}$$

10. $\log \frac{2}{7}$

$$\log 2 - \log 7$$

$$0.301 - 0.845$$

$$\boxed{-0.544}$$

11. $\log 7^{-3}$

~~$$\log 7^3$$~~
~~$$3 \log 7$$~~
~~$$-3 \log 7$$~~

$$-3(0.845) = \boxed{-2.535}$$

12. $\log 49$

$$\log (7 \cdot 7)$$

$$\log 7 + \log 7$$

$$(0.845) + 0.845$$

$$\boxed{1.690}$$