

Name: KEYTopic: 8.3: The number e

Date: _____

Summary:

Use a calculator to complete the table (round to the 3 decimal places)

n	10	10^2	10^3	10^4	10^5	10^6
$\left(1 + \frac{1}{n}\right)^n$	2.594	2.705	2.717	2.718	2.718	2.718

As n gets larger, $\left(1 + \frac{1}{n}\right)^n$ gets closer to 2.7182818459.

This is the value of e

e is also known as natural base e ; Euler number.

We can never forget the exponent properties!

$$a^m \cdot a^n = a^{m+n}$$

$$(a^m)^n = a^{mn}$$

$$(ab)^m = a^m b^m$$

$$a^{-m} = \frac{1}{a^m}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

These exponent rules are still applied when the base is e

Simplify the expression.

1. $e^3 \cdot e^4$

$$e^{3+4}$$

$$\boxed{e^7}$$

2. $\frac{10e^3}{5e^2}$

$$2e^{3-2}$$

$$\boxed{2e}$$

3. $(3e^{-4x})^2$

$$3^2 e^{-4x(2)}$$

$$9e^{-8x}$$

$$\boxed{\frac{9}{e^{8x}}}$$

4. $\frac{24e^8}{8e^5}$

$$3e^{8-5}$$

$$\boxed{3e^3}$$

5. $(2e^{-5x})^{-2}$

$$\frac{1}{(2e^{-5x})^2} =$$

$$\frac{1}{2^2 e^{-5x(2)}} = \frac{1}{4e^{-10x}}$$

$$\boxed{\frac{e^{10x}}{4}}$$

6. $e^{-2} \cdot e^8$

$$e^{-2+8} = \boxed{e^6}$$

7. $(2e^5)^3$

$$2^3 e^{5(3)} =$$

$$\boxed{8e^{15}}$$

8. $\frac{e^{-3}}{e^2}$

$$e^{-3-2}$$

$$e^{-5}$$

$$\boxed{\frac{1}{e^5}}$$

9. $-3e \cdot (4e)^{-2}$

$$\frac{-3e}{(4e)^2} = \frac{-3e}{4^2 e^2} =$$

$$\frac{-3e}{16e^2} = \frac{-3e^{1-2}}{16}$$

$$\frac{-3e^{-1}}{16} = \boxed{\frac{-3}{16e}}$$

11. $e^{2x} \cdot e^{1-2x}$

$$e^{2x+(1-2x)}$$

$$\boxed{e}$$

13. $e^2(2e^4)^3$

$$e^2 2^3 e^{4(3)}$$

$$e^2 8e^{12}$$

$$\boxed{8e^{14}}$$

10. $2e^x \cdot e^{(x+3)}$

$$\frac{2e^{x+(x+3)}}{2e^{2x+3}}$$

12. $\frac{e}{e^{(x+1)}}$

$$e^{1-(x+1)}$$

$$e^{1-x-1}$$

$$e^{-x}$$

$$\boxed{\frac{1}{e^x}}$$

14. $\left(\frac{e^2}{2}\right)^{-3}$

$$\frac{e^{2(-3)}}{2^{-3}} =$$

$$e^{-6} 2^3 =$$

$$\boxed{\frac{8}{e^6}}$$