

Algebra I 5.2 Relations and Functions

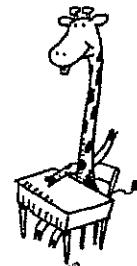
Name:

Relation: a set of ordered pairs. (Think "Relationship")

Ex.  $\{(2,4), (-3,1), (2,6)\}$

Giraffe Data

Age (years) $x$	Height (meters) $y$
18	4.25
20	4.4
21	5.25
14	5.00
18	4.85



Domain:  $x$ -values

Range:  $y$ -values

\* Put in order from least to greatest. List repeats once. Write in Set notation  $\{\}$ .

EX1 Find the domain and range of the ordered pairs listed for the giraffe data.

Domain:  $\{14, 18, 20, 21\}$

Range:  $\{4.25, 4.4, 4.85, 5.0, 5.25\}$

EX2 Find the domain and range of the relation represented by the data in the table.

Domain ( $x$ )	Range ( $y$ )
4	3
-2	1
-1	3
4	-2
-1	1

Domain =  
 $\{-2, -1, 4\}$

Range =  
 $\{-2, 1, 3\}$

Function: A relation that assigns exactly one value in the range to each value in the domain. (No repeating  $x$ 's).

Vertical Line Test: If any vertical line passes through more than 1 point on the graph, the relation is NOT a function.

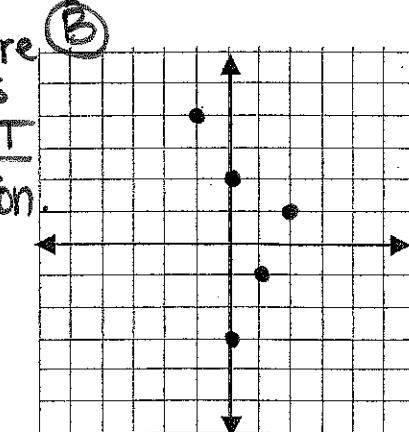
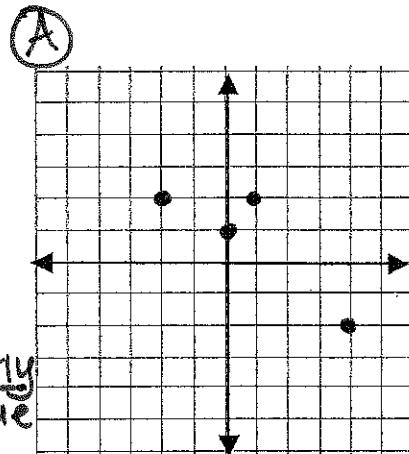
EX3 Use the vertical line test to determine whether each relation is a function. (graph data points)

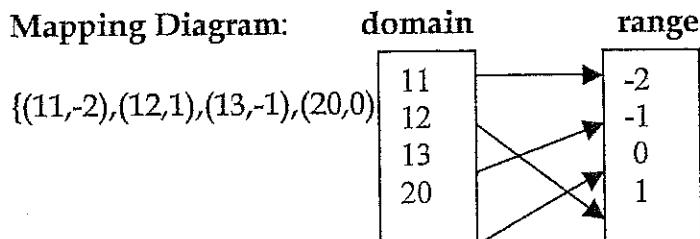
NOT a function.

a)  $\{(4,-2), (1,2), (0,1), (-2,2)\}$  Yes

b)  $\{(0,2), (1,-1), (-1,4), (0,-3), (2,1)\}$  No

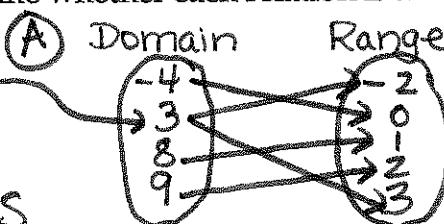
$x=0$  Repeats



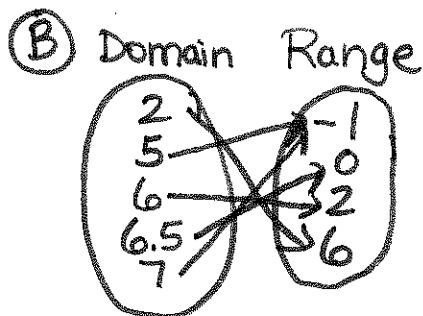


EX4 Use a mapping diagram to determine whether each relation is a function.

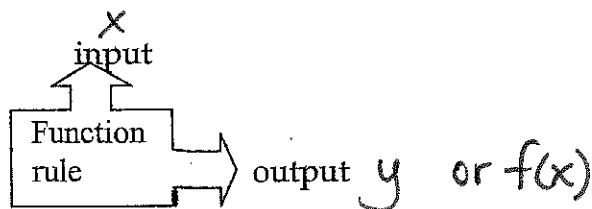
a)  $\{(3, -2), (8, 1), (9, 2), (3, 3), (-4, 0)\}$  NO



b)  $\{(6.5, 0), (7, -1), (6, 2), (2, 6), (5, -1)\}$  YES



Function Rule:



Function Notation:  $f(x)$

$$f(x) = y$$

EX5 Evaluate  $f(n) = -3n - 10$  for  $n=6$

$$\begin{aligned} f(6) &= -3(6) - 10 \\ &= -18 - 10 = \textcircled{-28} \end{aligned}$$

EX6 Evaluate  $f(x) = x^2 - 4$  for  $x=2.1$

$$f(2.1) = (2.1)^2 - 4 = 4.41 - 4 = \textcircled{.41}$$

EX7 Evaluate the function  $f(a) = -3a + 5$  to find the range for the domain  $\{-3, 1, 4\}$

$$\begin{aligned} f(-3) &= -3(-3) + 5 = 9 + 5 = 14 \\ f(1) &= -3(1) + 5 = -3 + 5 = 2 \\ f(4) &= -3(4) + 5 = -12 + 5 = -7 \end{aligned}$$

Range =  $\{-7, 2, 14\}$

EX8 Find the range of the function  $f(x) = x - 6$  for the domain  $\{-2, 0, 5\}$

$$\begin{aligned} f(-2) &= -2 - 6 = -8 \\ f(0) &= 0 - 6 = -6 \\ f(5) &= 5 - 6 = -1 \end{aligned}$$

Range =  $\{-8, -6, -1\}$