

Solving Multi-Step Equations

Additional Examples

Lesson 2-3

EXAMPLE Solve $3a + 6 + a = 90$.

$$4a + 6 = 90$$

$$4a + 6 - 6 = 90 - 6$$

$$4a = 84$$

$$\frac{4a}{4} = \frac{84}{4}$$

$$a = 21$$

Combine like terms.

Subtract 6 from each side.

Simplify.

Divide each side by 4.

Simplify.

Check: $3a + 6 + a = 90$

$$3(21) + 6 + 21 \stackrel{?}{=} 90$$

$$63 + 6 + 21 \stackrel{?}{=} 90$$

$$90 = 90 \checkmark$$

Substitute 21 for a.

EXAMPLE You need to build a rectangular pen in your back yard for your dog. One side of the pen will be against the house. Two sides of the pen have a length of x ft and the width will be 25 ft. What is the greatest length the pen can be if you have 63 ft of fencing?

Relate: $\boxed{\text{length of side}}$ plus 25 ft plus $\boxed{\text{length of side}}$ equals amount of fencing

Define: Let \boxed{x} = length of a side adjacent to the house.

Write: $\boxed{x} + 25 + \boxed{x} = 63$

$$x + 25 + x = 63$$

$$2x + 25 = 63$$

Combine like terms.

$$2x + 25 - 25 = 63 - 25$$

Subtract 25 from each side.

$$2x = 38$$

Simplify.

$$\frac{2x}{2} = \frac{38}{2}$$

Divide each side by 2.

$$x = 19$$

The pen can be 19 ft long.

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3 EXAMPLE Solve $2(x - 3) = 8$.

$$\begin{aligned} 2x - 6 &= 8 && \text{Use the Distributive Property.} \\ 2x - 6 + 6 &= 8 + 6 && \text{Add 6 to each side.} \\ 2x &= 14 && \text{Simplify.} \\ \frac{2x}{2} &= \frac{14}{2} && \text{Divide each side by 2.} \\ x &= 7 && \text{Simplify.} \end{aligned}$$

4 EXAMPLE Solve $\frac{3x}{2} + \frac{x}{5} = 17$.

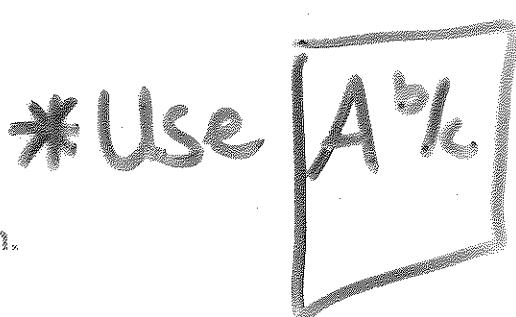
Method 1: Finding common denominators

$$\begin{aligned} \frac{3x}{2} + \frac{x}{5} &= 17 \\ \frac{3}{2}x + \frac{1}{5}x &= 17 \\ \frac{15}{10}x + \frac{2}{10}x &= 17 \\ \frac{17}{10}x &= 17 \end{aligned}$$

$$\cancel{\frac{10}{17}}\left(\frac{17}{10}x\right) = \cancel{\frac{10}{17}}(17)$$

$$x = 10$$

Rewrite the equation.



A common denominator of $\frac{3}{2}$ and $\frac{1}{5}$ is 10.

Combine like terms.

Multiply each side by the reciprocal of $\frac{17}{10}$, which is $\frac{10}{17}$.

Simplify.

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4 EXAMPLE (continued)

Method 2: Multiplying to clear fractions

$$\frac{3x}{2} + \frac{x}{5} = 17$$

$10\left(\frac{3x}{2} + \frac{x}{5}\right) = 10(17)$ Multiply each side by 10, a common multiple of 2 and 5.

$$10\left(\frac{3x}{2}\right) + 10\left(\frac{x}{5}\right) = 10(17)$$
 Use the Distributive Property.
$$15x + 2x = 170$$
 Multiply.
$$17x = 170$$
 Combine like terms.
$$\frac{17x}{17} = \frac{170}{17}$$
 Divide each side by 17.
$$x = 10$$
 Simplify.

5 EXAMPLE Solve $0.6a + 18.65 = 22.85$.

$$100(0.6a + 18.65) = 100(22.85)$$

The greatest number of decimal places is two places. Multiply each side by 100.

$$100(0.6a) + 100(18.65) = 100(22.85)$$
 Use the Distributive Property.
$$60a + 1865 = 2285$$
 Simplify.
$$60a + 1865 - 1865 = 2285 - 1865$$
 Subtract 1865 from each side.
$$60a = 420$$
 Simplify.
$$\frac{60a}{60} = \frac{420}{60}$$
 Divide each side by 60.
$$a = 7$$
 Simplify.